

## FY BSc SEM II MATHS PAPER II SAMPLE QUESTIONS

Q Choose correct alternative in each of the following

1. Which of the following is not a solution to the system  $6x+4y=0$ 
  - (a)  $(-2, 3)$
  - (b)  $(6, -4)$
  - (c)  $(4, -6)$
  - (d)  $(2, -3)$
2. Which of the following sets is Linearly Independent?
  - (a)  $\{(7, 5), (14, 10)\}$
  - (b)  $\{(7, 5), (5, 7)\}$
  - (c)  $\{(7, 5), (352, 252)\}$
  - (d)  $\{(7, 5), (5, 7), (12, 12)\}$
3. The Nullity of the Linear transformation  $T:\mathbb{R}^2\rightarrow\mathbb{R}^2$  defined as  $T(x, y) = (0, 0)$  is
  - (a) 0
  - (b) 1
  - (c) 2
  - (d) 3
4. If for a Linear transformation  $T:\mathbb{R}^4\rightarrow\mathbb{R}^3$  the Rank of  $T=3$  then the  $\text{Dim}(\text{Ker}(T))=?$ 
  - (a) 2
  - (b) 3
  - (c) 1
  - (d) 0

5. For which value of  $k$  does the following system have infinitely many solutions?

$$2x - y = k, 4x - 2y = 6$$

- (a) 3
- (b) 6
- (c) 1
- (d) 2

6. Which of the following set is a generating set of  $\mathbb{R}^3$ ?

- (a)  $\{(1, 2, 0), (0, 1, 1), (-1, 0, 1)\}$
- (b)  $\{(1, 2, 1), (2, 4, 2), (-1, 0, 1)\}$
- (c)  $\{(1, 1, 0), (0, 1, 1)\}$
- (d)  $\{(-1, 0, 1), (0, 1, 1), (0, 0, 0)\}$

7. If for a linear transformation  $\text{Rank } T = 4$  then the nullity of  $T$  is

- (a) 3
- (b) 5
- (c) 0
- (d) None of these

8. Which of the following is not a solution to the system  $5x - y = 0$ ?

- (a) (1, 5)
- (b) (-1, -5)
- (c) (-2, -10)
- (d) (-1, 5)

9. Which of the following sets is linear dependent?

- (a)  $\{(1, 1), (-1, 1)\}$
- (b)  $\{(1, 2), (2, 1)\}$
- (c)  $\{(3, 34), (0, 3)\}$
- (d)  $\{(3, 3), (2, 2)\}$

10. If for a linear transformation  $T: \mathbb{R}^4 \rightarrow \mathbb{R}^3$  the  $\text{Dim}(\text{Im}(T)) = 2$  then the nullity of  $T$  is
- (a) 2
  - (b) 4
  - (c) 1
  - (d) 3
11. A system of linear equation is inconsistent, if it
- (a) is solvable
  - (b) is not solvable
  - (c) has unique solution
  - (d) has infinite solution
12. Homogenous system of linear equations always has
- (a) no solution
  - (b) a trivial solution
  - (c) a non trivial solution
  - (d) infinite solution
13. System of  $m$  linear equation in  $n$  variables, having  $r$  as the number of its pivot elements, Which one of the following possibilities is never true?
- (a)  $r \leq m$
  - (b)  $r < n$
  - (c)  $r = n$
  - (d)  $r > n$
14. System mentioned above is consistent, then it has infinite solution, if
- (a)  $r < n$
  - (b)  $r = n$
  - (c)  $r > n$
  - (d) none of the above

15. A system of linear equations given by

$$\begin{bmatrix} 1 & 2 \\ 0 & 3 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 3 \end{bmatrix}$$

- (a) is consistent
- (b) is inconsistent
- (C) has zero solution
- (d) has many solution

16. A Singleton set  $\{ 0 \}$  can never be a vector space under any operations, because

- (a) it is finite set
- (b) it has nothing worth in it
- (c) one cant have + and  $\bullet$  on zero
- (d) this is a false statement

17. The set of all irrational numbers under the usual + and  $\bullet$  , is not a vector space over  $\mathbb{R}$  because

- (a) it is not closed under +
- (b) it is not close number  $\bullet$
- (c) it does not have zero
- (d) All of the above

18. The singleton set  $\{ 0 \}$  of any vector space  $V$  is

- (a) Linearly independent
- (b) Linearly dependent
- (c) Neither linearly dependent nor independent
- (d) Depends on the vector space  $V$

19. The empty set  $\phi$  of any vector space  $V$  is

- (a) Linearly independent
- (b) Empty means nothing, nothing means zero,  $\therefore$  linearly dependent
- (c) Neither dependent not independent
- (d) Depends on the nature of the vector space  $V$

20.  $V$  is a vector space over  $\mathbb{R}$ .  $S$  is linearly independent set of vector from  $V$ . Then

- (a) Every subset of  $V$ , is linearly independent
- (b) Every subset of  $V$ , is linearly dependent
- (c) Every subset of  $S$ , is linearly independent
- (d) Every subset of  $S$ , is linearly dependent

21.  $V$  is a vector space over  $\mathbb{R}$ .  $S$  is linearly dependent set of vector from  $V$ . Then

- (a) Every subset of  $V$ , is linearly independent
- (b) Every subset of  $S$ , is linearly independent
- (c) Every subset of  $V$ , is linearly dependent
- (d) Every subset of  $S$ , is linearly dependent

22. A linear transformation is basically

- (a) A linear equation
- (b) A system of linear equation
- (c) A line in geometry
- (d) A mapping between two vector spaces

23.  $T : \mathbb{R}^2 + \mathbb{R}^3$ , defined as  $T(x, y) = (1, 2, 3), \forall (x, y) \in \mathbb{R}^2$  is not a linear transformation because

- (a)  $T$  is not defined properly
- (b)  $T$  is not function
- (c)  $(0, 0)$  of  $\mathbb{R}^2 \rightarrow (0, 0, 0)$  of  $\mathbb{R}^3$
- (d) where does  $(1, 2, 3)$  come from?

24.  $V$  and  $V'$  are two vector spaces with their respective zero as  $0$  and  $0'$ .

$T : V \rightarrow V'$  is a linear transformation, given by  $T(u) = 0', \forall u \in V$ . Then

- (a)  $\text{Ker } T = \{ 0 \}, \text{ Im } T = \{ 0' \}$
- (b)  $\text{Ker } T = \{ 0 \}, \text{ Im } T = V'$
- (c)  $\text{Ker } T = V, \text{ Im } T = \{ 0' \}$
- (d)  $\text{Ker } V, \text{ Im } T = V'$

25.  $V$  is a vector space and  $T : V \rightarrow V$  is a linear transformation given by  $T(u) = u$ ,

$\forall u \in V$ . Then,

(a)  $\text{Ker } T = \{ 0 \}$ ,  $\text{Im } T = \{ 0 \}$

(b)  $\text{Ker } T = \{ 0 \}$ ,  $\text{Im } T = V$

(c)  $\text{Ker } T = V$ ,  $\text{Im } T = \{ 0 \}$

(d)  $\text{Ker } T = V$ ,  $\text{Im } T = V$